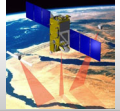


Natural variability in stage/discharge relationship: From in situ measurements to the SWOT satellite error estimates

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The SWOT mission

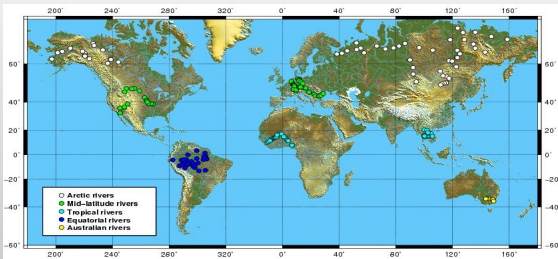
- The Surface Water Ocean Topography (SWOT) mission is a wide swath altimeter, with two 60 km swaths (with 10m to 70m across track resolution and 5m along track resolution). It will measure surface water elevation.
- 2 orbits have been considered:
 - Orbit 1: 20 day repeat period, 74° inclination and ~950km altitude.
 - Orbit 2: 22 day repeat period, 78° inclination and ~950km altitude.



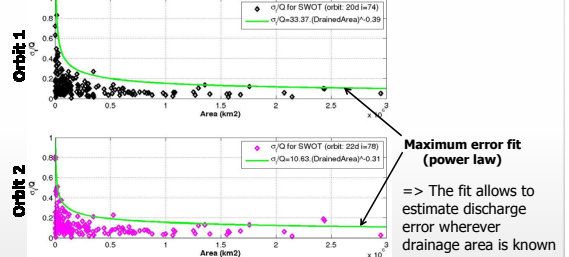
1. Error on the discharge due to the orbit temporal sampling

- (a) Hypothesis: SWOT measurement already converted in discharge
- (b) Methodology:
 - Gather in-situ daily discharges. Then extract the SWOT discharge time series (= dates where SWOT "see" the gauge).
 - Compute monthly mean discharge from daily (Q_m , our "truth") and SWOT (Q_{mSWOT}) time series and then the sampling error:

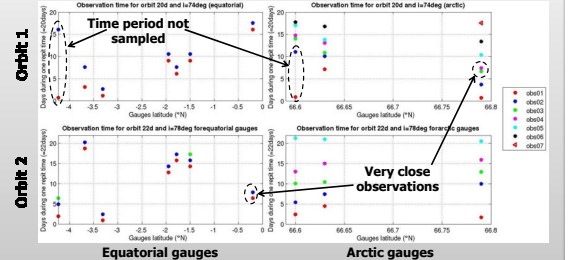
$$\frac{\sigma_Q}{Q} = \frac{\text{std}(Q_m(\text{month}) - Q_{mSWOT}(\text{month}))}{\text{mean}(Q_m)}$$
 - Classify these errors as a function of the river drainage area at the gauge location and then fit a relationship between the error and the drainage area.
- (c) Gauges used (from USGS, GRDC, ANA & HyBAM)



- (d) Results: errors due to the orbit temporal sampling vs drainage area
 - Orbit 1: σ_Q/Q for SWOT (orbit 20d i=74) vs Area (km²). Fit: $\sigma_Q/Q = 0.37 \cdot (\text{DrainedArea})^{-0.39}$
 - Orbit 2: σ_Q/Q for SWOT (orbit 22d i=78) vs Area (km²). Fit: $\sigma_Q/Q = 0.63 \cdot (\text{DrainedArea})^{-0.31}$



- (e) Remark: some high errors because not constant SWOT time sampling



2. Error on the discharge due to the measurement error

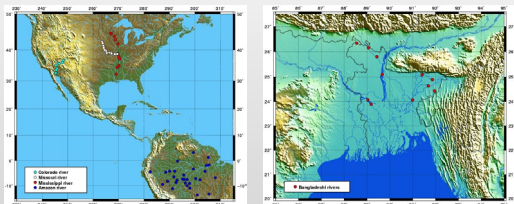
- (a) Hypothesis: Power law relationship between discharge (Q) and river depth (D): $Q = c \cdot D^b$ and $D = h - h_0$, h is the elevation measured by SWOT and h_0 is the river bed elevation.
- (b) Methodology: gather in-situ stage and discharge measurements. Then compute the error on the discharge estimate:

$$\frac{\sigma_Q}{Q} = \sqrt{\eta^2 + \left(b \frac{\sigma_D}{D}\right)^2}$$

Model error (between true discharge and the one from power law) Error due to the measurement error (σ_D)

Then estimate the value of η , b and D at the gauge location and finally extrapolate these results everywhere along the river.

- (c) Gauges used (from USGS, GRDC, ANA & HyBAM):



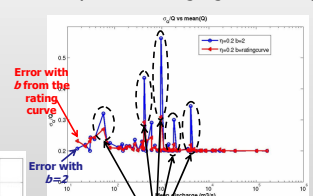
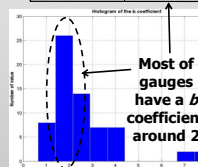
64 gauges in America

10 gauges in Bangladesh

- (d) On river where there is no gauges, the river depth (D) can be estimated by using a power law relationship between river depth and drainage area (Moody and Troutman, 2002).

- (e) Model error (η) vs SWOT ($b \cdot \sigma_D/D$) measurement error at the gauges location:
 - Error due to SWOT measurement is low.
 - Difficult to estimate model error (η): underestimate if discharge not directly measured (most gauges), overestimate if different flow regimes (needs at least two different power laws). Can be estimated ~20% (Dingman and Sharma, 1997; Bjerklie et al., 2003)
- (f) Estimate of the b coefficient for all rivers (even with no gauges available):
 - From the gauges:

River	Median(b)
Amazon	2.0
Brahmaputra	3.2
Colorado	2.5
Mississippi	1.6
Missouri	3.8
All rivers	2.3



Discharge error sensitive to the b coefficient only for low river depth ($D < 1m$)

=> For rivers with no gauges and not too low river depth, $b=2$ is a good approximation

Conclusion

- Importance of the SWOT temporal sampling on the computation of monthly discharge.
- SWOT spatio-temporal errors have been computed from in-situ networks and for different satellite orbits.
- General hydrological parameters have been derived from these analysis.
- These parameters could be used to generate discharge error maps for a global river network.